

Practicing Time Analysis

- Consider the following static method:

```
public static int mystery(int n) {  
    int x = 0;  
    for (int i = 0; i < n; i++) {  
        x += i;           // statement 1  
        for (int j = 0; j < i; j++) {  
            x += j;  
        }  
    }  
    return x;  
}
```

- What is the big-O expression for the number of times that statement 1 is executed as a function of the input n ?
 - the outer loop performs n repetitions
 - statement 1 is executed once for every repetition – n times!
 - n is $O(n)$!

What about now?

- Consider the following static method:

```
public static int mystery(int n) {  
    int x = 0;  
    for (int i = 0; i < 3*n + 4; i++) {  
        x += i;           // statement 1  
        for (int j = 0; j < i; j++) {  
            x += j;  
        }  
    }  
    return x;  
}
```

- What is the big-O expression for the number of times that statement 1 is executed as a function of the input n ?
 - the outer loop performs $3*n + 4$ repetitions
 - statement 1 is executed once for every repetition: $3*n+4$ times!
 - $3*n + 4$ is $O(n)$!

Practicing Time Analysis

- Consider the following static method:

```
public static int mystery(int n) {
    int x = 0;
    for (int i = 0; i < n; i++) {
        x += i;           // statement 1
        for (int j = 0; j < i; j++) {
            x += j;       // statement 2
        }
    }
    return x;
}
```

- What is the big-O expression for the number of times that statement 2 is executed as a function of the input n ?
 - the outer loop performs n repetitions
 - the inner loop performs i repetitions

Practicing Time Analysis

- Consider the following static method:

```
public static int mystery(int n) {
    int x = 0;
    for (int i = 0; i < n; i++) {
        x += i;           // statement 1
        for (int j = 0; j < i; j++) {
            x += j;       // statement 2
        }
    }
    return x;
}
```

- What is the big-O expression for the number of times that statement 2 is executed as a function of the input n ?

<u>value of i</u>	<u>number of times statement 2 is executed</u>	
0	0	} $1 + 2 + \dots + n - 1 = O(n^2)$ (as we saw in selection sort!)
1	1	
...	...	
$n - 1$	$n - 1$	